

Let "small" = 2cm



①

Its boundary layer becomes turbulent at
 $R = 100\,000$

Reynold's number:

$$R = \frac{\rho L v}{\eta}$$

$$\rho = 1000 \text{ kg m}^{-3}$$

$$L = 2 \times 10^{-2} \text{ m}$$

$$\eta = 0.001 \text{ Pa s}$$

$$v = ?$$

$$v = \frac{R \eta}{\rho L}$$

$$= \frac{100\,000 \times 0.001}{1000 \times 2 \times 10^{-2}}$$

$$v = 5 \text{ ms}^{-1}$$

Make reasonable
assumptions
requirement

Poiseuille's law: $\frac{V}{t} = \frac{\pi \Delta p D^4}{128 L \eta}$

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so $\Delta p_{\text{healthy}} = \frac{V \times 128 \times L \times \eta}{t \times \pi \times D^4}$

$\Delta p_{\text{tight}} = \frac{V \cdot 128 \cdot L \cdot \eta}{t \cdot \pi (0.95D)^4}$

$= \frac{V \cdot 128 \cdot L \cdot \eta}{t \cdot \pi D^4}$
Same long substitution

$0.95^4 = 0.851$

so $\Delta p_{\text{tight}} = \frac{\Delta p_{\text{healthy}}}{0.851}$

$= \frac{\Delta p_{\text{healthy}}}{0.95^4}$

$\Delta p_{\text{tight}} = 1.23 \Delta p_{\text{healthy}}$

Use of subscripts to distinguish quantities

$$\frac{V}{t} = \frac{\pi \Delta p \cdot D^4}{128 \cdot L \cdot \eta}$$

(3)

Let $V_{01} = 0.5 \text{ m}^3$ and $180 \text{ s} = t$ More "reasonable assumptions. I've never timed a bottle

so $\frac{0.5}{t_{H_2O}} = \frac{k}{0.001}$ where $k = \frac{\pi \Delta p D^4}{128 L}$

Bundle everything that doesn't change into a single constant

$$t_{H_2O} = \frac{0.5 \times 0.001}{k}$$

$$t_{O_1} = \frac{0.5}{k} \times 0.084 \text{ Pa}$$

$$\text{so } t_{O_1} = 84 t_{H_2O}$$

Question doesn't ask for exact time, just how many times longer

$$L = 0.6 \text{ m}$$

$$\rho = 1000 \text{ kg m}^{-3}$$

$$v = ?$$

$$\eta = 0.001 \text{ Pa s}$$

$$R_{\text{lim}} = 2000$$

More dodgy ^④
assumptions

I've never measured
a canoe

R based on no
turbulence AT ALL

$$R_{\text{lim}} = \frac{\rho L v}{\eta}$$

$$\text{so } v_{\text{lim}} = \frac{R_{\text{lim}} \eta}{\rho L}$$

$$= \frac{2000 \times 0.001}{1000 \times 0.6}$$

$$= 3.3 \times 10^{-3} \text{ ms}^{-1}$$

i.e. 12 m per hour

Result seems
dodgy but
I think my
maths is OK

$$\frac{V}{t} = \frac{\pi \Delta p D^4}{128 L \eta} \quad \text{--- ①}$$

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let 2 cup = 300 ml
unit conversion:

$$1 \text{ m}^3 = 10^3 \text{ L so } 1 \text{ L} = \frac{1}{10^3} = 0.001 \text{ m}^3 \quad \text{L in this line is liter}$$

$$\text{so } 1 \text{ cup} = 300 \times 10^{-3} \times 10^{-3} = 0.3 \times 10^{-3} \text{ m}^3$$

$$\text{let } t = 5 \text{ s}$$

From ①

$$\frac{\eta}{t} = \frac{\pi \Delta p D^4}{128 L V}$$

$$\text{so for water, } \frac{\eta}{t_{\text{H}_2\text{O}}} = \frac{0.001}{5} = 0.0002$$

$\pi, \Delta p, D^4, 128, L \text{ \& } Vol$ are unchanged

and for honey

$$\frac{\eta}{t} = \frac{1000}{t_{\text{hon}}} = 0.0002$$

$$t_{\text{hon}} = \frac{1000}{0.0002} = 5 \times 10^6 \text{ s}$$

i.e about 58 days

oo bee keepers use ~ 6cm diameter funnels

$$D = 1 \times 10^{-2} \text{ m}$$

$$R = 2000$$

$$\rho = 918 \text{ kg m}^{-3}$$

$$\eta = 0.084 \text{ Pa s}$$

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$$R = \frac{\rho L v}{\eta}$$

$$v = \frac{R \eta}{\rho L}$$

$$= \frac{2000 \times 0.084}{918 \cdot 1 \times 10^{-2}}$$

$$v = 18.3 \text{ m s}^{-1}$$

Conclusion: don't use a 1cm diameter stick to mix olive oil when blending it.

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$$L = 15 \text{ m}$$

$$\rho = 1.25 \text{ kg m}^{-3}$$

$$\eta = 0.0000183 \text{ Pa s}$$

$$v = ?$$

$$R_{\text{lim}} = 2000$$

$$v = \frac{R_{\text{lim}} \eta}{\rho L}$$

$$= \frac{2000 \times 0.0000183}{15 \times 1.25}$$

$$v = 1.95 \times 10^{-3} \text{ m s}^{-1}$$

$$\text{i.e. } 2 \text{ mm s}^{-1}$$

Does this matter?

No.

Blimps contain lighter than air gas, (helium?) and don't rely on wings to float in air; only as control surfaces.